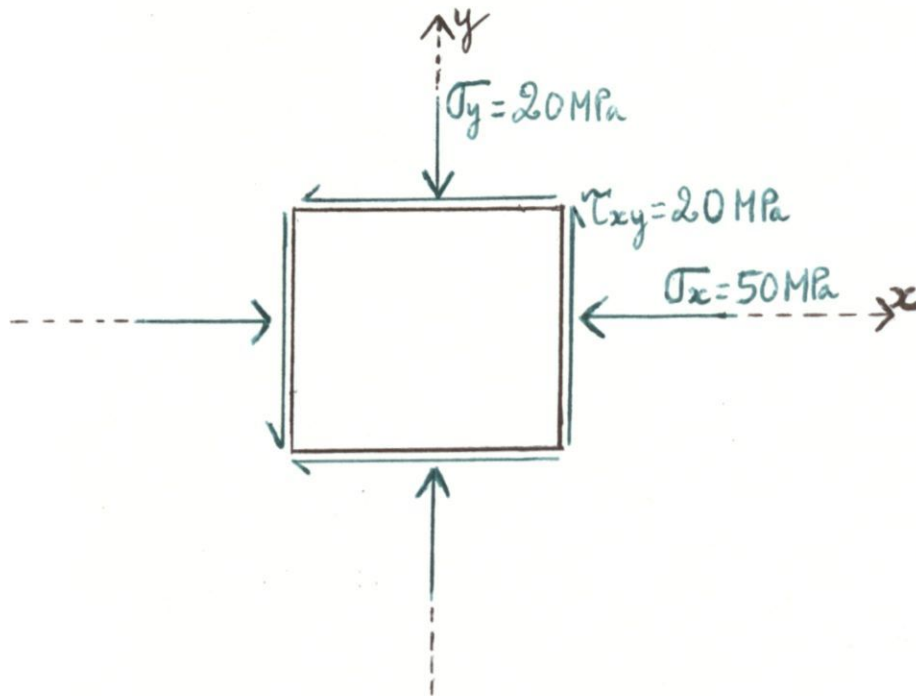
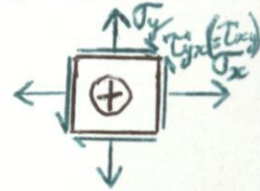


Date: 7<sup>th</sup> January 2019



Positive sign convention



$$\begin{aligned}\sigma_y &= -20 \text{ MPa} \\ \sigma_x &= -50 \text{ MPa} \\ \tau_{xy} &= 20 \text{ MPa}\end{aligned}$$

$$\sigma_{avg} = \frac{\sigma_x + \sigma_y}{2} = \frac{[-50] + [-20]}{2} \text{ MPa} = -35 \text{ MPa} ; C(\sigma_{avg}, 0) \Rightarrow C(-35 \text{ MPa}, 0)$$

$$\tau_{MAX} = R = \sqrt{\left(\frac{\sigma_x - \sigma_y}{2}\right)^2 + (\tau_{xy})^2} = \sqrt{\left[\frac{(-50) - (-20)}{2}\right]^2 + (20)^2} = 25 \text{ MPa}$$

$$\sigma_1 = \sigma_{avg} + R = (-35 \text{ MPa}) + (25 \text{ MPa}) = -10 \text{ MPa}$$

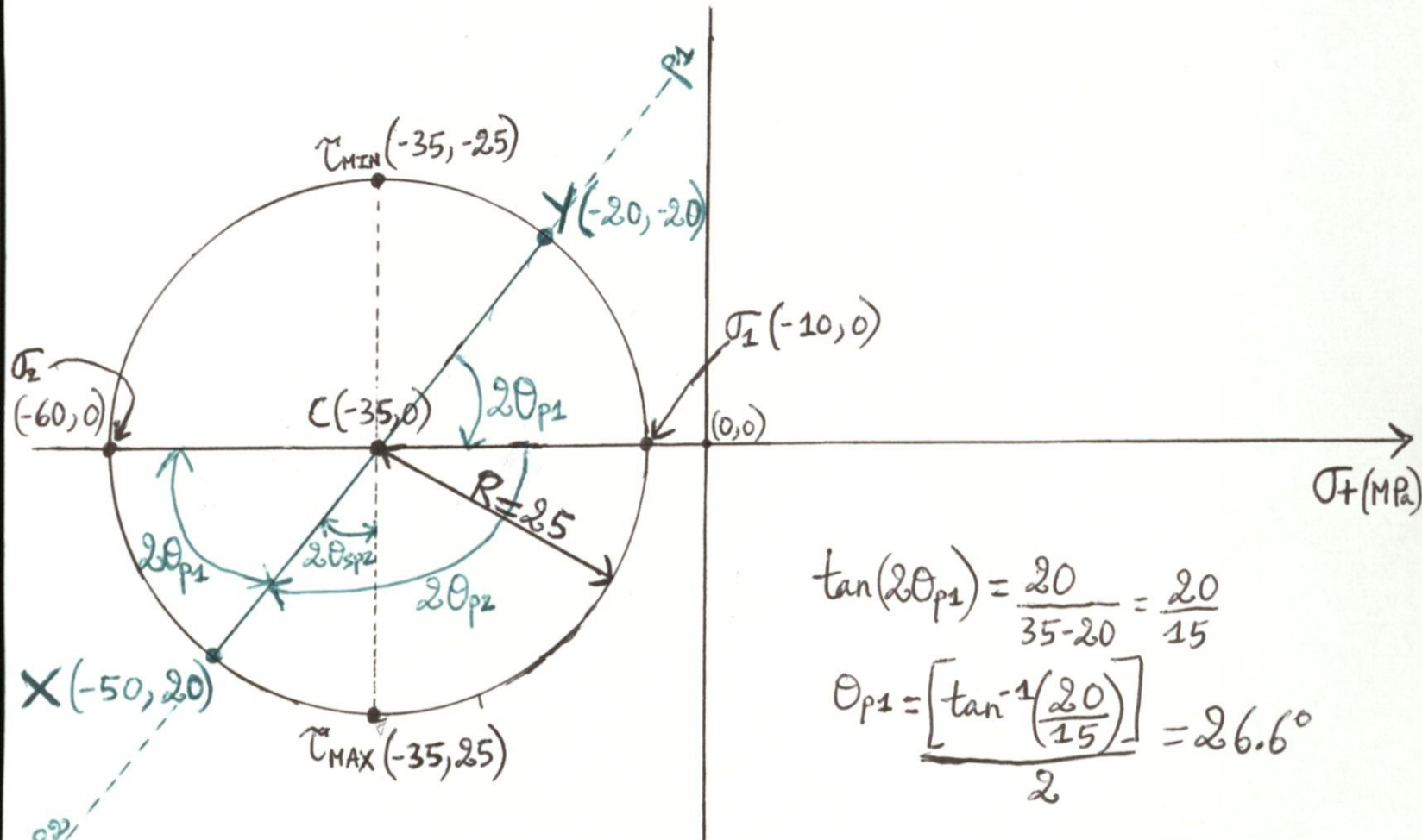
$$\sigma_2 = \sigma_{avg} - R = (-35 \text{ MPa}) - (25 \text{ MPa}) = -60 \text{ MPa}$$

$$X(\sigma_x, \tau_{xy}) \Rightarrow X(-50 \text{ MPa}, 20 \text{ MPa})$$

$$Y(\sigma_y, -\tau_{xy}) \Rightarrow Y(-20 \text{ MPa}, -20 \text{ MPa})$$

Date: 7<sup>th</sup> January 2019

## Mohr's Circle



$$\tan(2\theta_{p1}) = \frac{20}{35-20} = \frac{20}{15}$$

$$\theta_{p1} = \frac{\left[ \tan^{-1}\left(\frac{20}{15}\right) \right]}{2} = 26.6^\circ$$

$$2\theta_{spz} = 90^\circ - 2\theta_{p1} = 90 - 2(26.6) = 36.87^\circ$$

$$2\theta_{p2} = (90^\circ) + 2\theta_{spz} = 90^\circ + 36.87^\circ = 126.87^\circ$$

$$\theta_{p2} = \frac{126.87^\circ}{2} = 63.4^\circ$$