

At A & D $\Rightarrow \tau = 0$

| Section | b (mm) | h (mm) | \tilde{y} (mm) | A (mm ²) | $\tilde{y}A$ (mm ³) | d (mm) = $ \tilde{y} - \bar{y} $ |
|---------|--------|--------|-----------------------------|----------------------|---------------------------------|----------------------------------|
| ① | 175 | 700 | 350 | 122,500 | 42,875,000 | 202.25 |
| ② | 1,000 | 200 | $700 + \frac{200}{2} = 800$ | 200,000 | 160,000,000 | 247.75 |
| ③ | 175 | 700 | 350 | 122,500 | 42,875,000 | 202.25 |

$\Sigma A = 445,000$ $\Sigma \tilde{y}A = 245,750,000$

$$\bar{y} = \frac{\Sigma \tilde{y}A}{\Sigma A} = \frac{245,750,000 \text{ mm}^3}{445,000 \text{ mm}^2} = 552.25 \text{ mm}$$

$$I_{①} = I_{③} = \frac{bh^3}{12} + Ad^2 = \frac{(175)(700)^3}{12} + (122,500)(202.25)^2 = 1.001295349 \times 10^{10} \text{ mm}^4$$

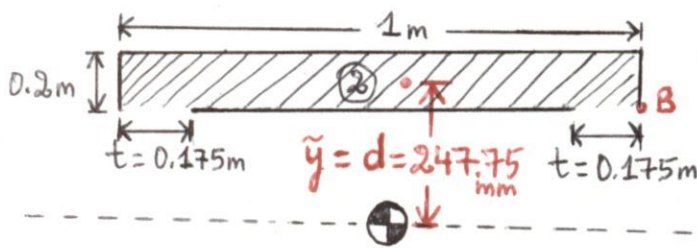
$$I_{②} = \frac{bh^3}{12} + Ad^2 = \frac{(1,000)(200)^3}{12} + (200,000)(247.75)^2 = 1.294267917 \times 10^{10} \text{ mm}^4$$

$$I_{\text{Tot}} = I_{①} + I_{②} + I_{③} = (1.001295 \times 10^{10})(2) + (1.29426 \times 10^{10}) = 3.296858615 \times 10^{10} \text{ mm}^4$$

$$= 3.296858615 \times 10^{10} \text{ mm}^4 \left(\frac{1 \times 10^{-12} \text{ m}^4}{1 \text{ mm}^4} \right) = 0.03296858615 \text{ m}^4$$

Date: 6th March 2019

Shear Stress at point B, τ_B



$$V = 65 \text{ kN}$$

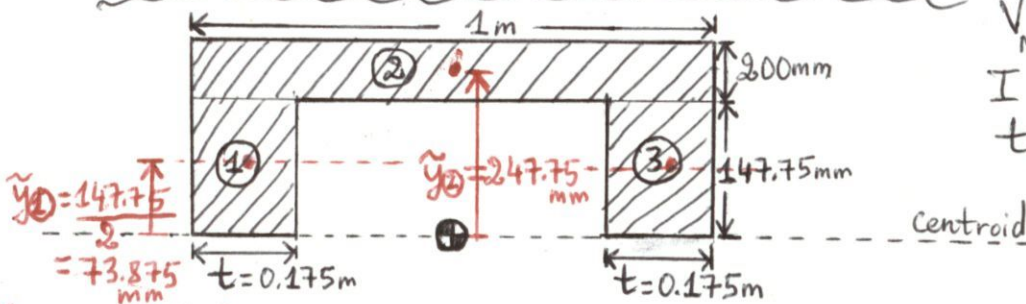
$$I = 0.03296858615 \text{ m}^4$$

$$t_B = 0.175 + 0.175 = 0.35 \text{ m}$$

$$Q_B = \sum \tilde{y}A = (0.24775 \text{ m})(0.2 \text{ m})(1 \text{ m}) = 0.04955 \text{ m}^3$$

$$\tau_B = \frac{V Q_B}{I t_B} = \frac{(65 \text{ kN})(0.04955 \text{ m}^3)}{(0.03296858615 \text{ m}^4)(0.35 \text{ m})} = 279.119 \text{ kPa}$$

Shear Stress at point C, Centroid, $\tau_C = \tau_{MAX}$



$$V_{MAX} = 65 \text{ kN}$$

$$I = 0.03296858615 \text{ m}^4$$

$$t_C = 0.175 + 0.175 = 0.35 \text{ m}$$

$$Q_2 = \tilde{y}_2 A_2 = (0.24775 \text{ m})(0.2 \text{ m})(1 \text{ m}) = 0.04955 \text{ m}^3$$

$$Q_1 = Q_3 = \tilde{y}_1 A_1 = \tilde{y}_3 A_3 = (0.14775 \text{ m})(0.175 \text{ m})(0.073875 \text{ m}) = 1.910130469 \times 10^{-3} \text{ m}^3$$

$$Q_C = \sum \tilde{y}A = Q_2 + Q_1 + Q_3 = (0.04955) + (2)(1.910130469 \times 10^{-3}) = 0.05337026 \text{ m}^3$$

$$\tau_C = \frac{V_{MAX} Q_C}{I t_C} = \frac{(65 \text{ kN})(0.05337026 \text{ m}^3)}{(0.03296858615 \text{ m}^4)(0.35 \text{ m})} = 300.64 \text{ kPa} \approx 301 \text{ kPa}$$